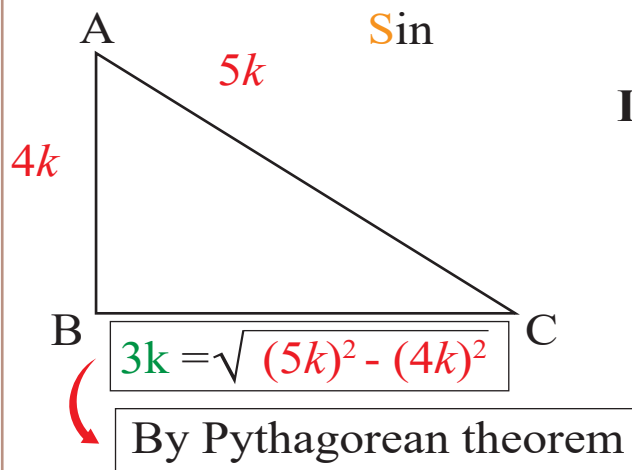
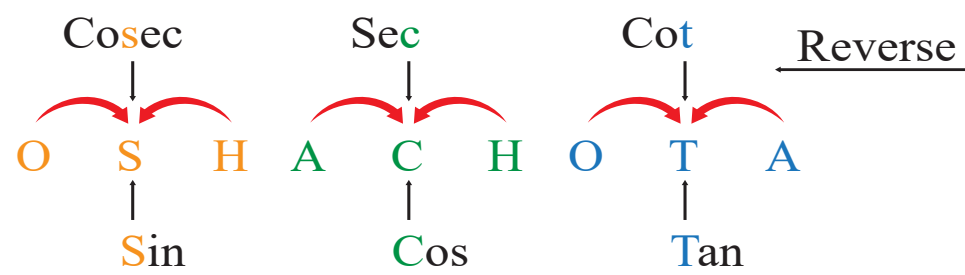


TRIGONOMETRY AT A GLANCE

Trigonometric ratio's in right angled triangle:

Remember "OSHACHOTA".



If $\sin A = \frac{4}{5}$, then

$$\begin{aligned} \sin C &= \frac{4}{5} = \frac{4k}{5k} = \frac{O}{H} \\ \text{> } \cos C &= \frac{A}{H} = \frac{3k}{5k} = \frac{3}{5} \\ \text{> } \tan C &= \frac{O}{A} = \frac{4k}{3k} = \frac{4}{3} \\ \text{> } \cot C &= \frac{A}{O} = \frac{3k}{4k} = \frac{3}{4} \\ \text{> } \sec C &= \frac{H}{A} = \frac{5k}{3k} = \frac{5}{3} \\ \text{> } \text{cosec } C &= \frac{H}{O} = \frac{5k}{4k} = \frac{5}{4} \end{aligned}$$

Trigonometric ratio of complementary angles:

Sine and Cosine are **complementary** of each other.
 $\sin(90^\circ - \theta) = \cos \theta$ and $\cos(90^\circ - \theta) = \sin \theta$.

Tangent and Cotangent are **complementary** of each other.
 $\tan(90^\circ - \theta) = \cot \theta$ and $\cot(90^\circ - \theta) = \tan \theta$.

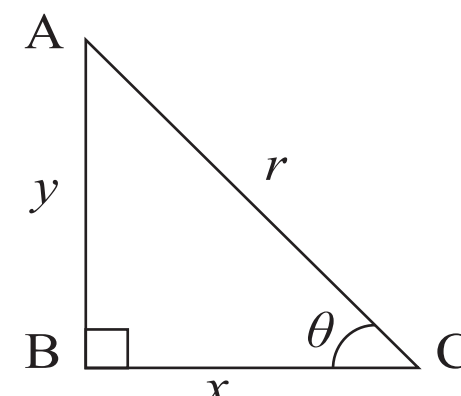
Secant and Cosecant are **complementary** of each other.
 $\sec(90^\circ - \theta) = \text{cosec } \theta$ and $\text{cosec}(90^\circ - \theta) = \sec \theta$.

Relation among trigonometric ratio's:

$\tan \theta$	$\cot \theta$	$\sec \theta$	$\text{cosec } \theta$
\downarrow	\downarrow	\downarrow	\downarrow
$\frac{\sin \theta}{\cos \theta}$	$\frac{\cos \theta}{\sin \theta}$	$\tan \theta \times \text{cosec } \theta$	$\frac{\sec \theta}{\tan \theta}$
\downarrow	\downarrow	\downarrow	\downarrow
$\frac{1}{\cot \theta}$	$\frac{1}{\tan \theta}$	$\frac{1}{\cos \theta}$	$\frac{1}{\sin \theta}$
\downarrow	\downarrow	\downarrow	\downarrow
$\frac{\sec \theta}{\text{cosec } \theta}$	$\frac{\text{cosec } \theta}{\sec \theta}$	$\frac{\text{cosec } \theta}{\cot \theta}$	$\sec \theta \times \cot \theta$

Identities:

$$\begin{aligned} \sin \theta &= \frac{y}{r} \Rightarrow \sin^2 \theta = \frac{y^2}{r^2} \\ \cos \theta &= \frac{x}{r} \Rightarrow \cos^2 \theta = \frac{x^2}{r^2} \\ \sin^2 \theta + \cos^2 \theta &= \frac{y^2}{r^2} + \frac{x^2}{r^2} = \frac{y^2 + x^2}{r^2} \\ &= \frac{r^2}{r^2} \quad [\text{By Pythagorean theorem}] \\ &= 1 \end{aligned}$$



$$\sin^2 \theta + \cos^2 \theta = 1$$

Similarly,

$$\sec^2 \theta - \tan^2 \theta = 1$$

$$\text{cosec}^2 \theta - \cot^2 \theta = 1$$

Identities

$\sin^2 \theta + \cos^2 \theta = 1$	$\sec^2 \theta - \tan^2 \theta = 1$	$\text{cosec}^2 \theta - \cot^2 \theta = 1$
\downarrow	\downarrow	\downarrow
$1 + \cos^2 \theta = \sin^2 \theta$	$1 + \tan^2 \theta = \sec^2 \theta$	$1 + \cot^2 \theta = \text{cosec}^2 \theta$
\downarrow	\downarrow	\downarrow
$1 - \sin^2 \theta = \cos^2 \theta$	$\sec^2 \theta - 1 = \tan^2 \theta$	$\text{cosec}^2 \theta - 1 = \cot^2 \theta$

Trigonometric ratios of standard angles:

Standard Angles (θ)	0°	30°	45°	60°	90°
	0	1	2	3	4
	$\frac{0}{4} = 0$	$\frac{1}{4}$	$\frac{2}{4} = \frac{1}{2}$	$\frac{3}{4}$	$\frac{4}{4} = 1$
$\sin \theta$	$\sqrt{0} = 0$	$\sqrt{\frac{1}{4}} = \frac{1}{2}$	$\sqrt{\frac{2}{4}} = \frac{1}{\sqrt{2}}$	$\sqrt{\frac{3}{4}} = \frac{\sqrt{3}}{2}$	$\sqrt{1} = 1$
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	Not define
$\cot \theta$	Not define	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0
$\sec \theta$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	Not define
$\text{cosec } \theta$	Not define	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}}$	1

Write numbers from 0 to 4.

Divide all by 4.

Find square root.

Write the values in reverse order.

Use: $\tan \theta = \frac{\sin \theta}{\cos \theta}$

Write the values in reverse order.

Use: $\tan \theta = \frac{\sin \theta}{\cos \theta}$

Write the values in reverse order.